

4.6 Independence

Study Ch. 4.6, p. 202 # 115,119

Class Notes: Prof. G. Battaly, Westchester Community College, NY

 [Statistics Home Page](#)

©Gertrude Battaly, 2010

 [Class Notes](#)

4.6 Independence

Conditional Probability Rule:

If A and B are any two events with $P(A) > 0$,

$$\text{then } P(B/A) = \frac{P(A\&B)}{P(A)}$$

The probability that event B occurs,
under the condition that
it is given that event A has occurred.

Class Notes: Prof. G. Battaly, Westchester Community College, NY

 [Statistics Home Page](#)

©Gertrude Battaly, 2010

 [Class Notes](#)

4.6 Independence

INDEPENDENT EVENTS:

Event B is **INDEPENDENT** of event A

if:

$$P(B/A) = P(B)$$

also:

$$P(A/B) = P(A)$$

Two events are independent if:
the occurrence of one does not change the probability of the occurrence of the other.

Class Notes: Prof. G. Battaly, Westchester Community College, NY

 [Statistics Home Page](#)

©Gertrude Battaly, 2010

 [Class Notes](#)

4.6 Independence

p. 203 # 116

	Location of injury			
	Work	Home	Other	Total
Male	8	9.8	17.8	35.6
Female	1.3	11.6	12.9	25.8
Total	9.3	21.4	30.7	61.4

Find:

- $P(\text{Work})$
- $P(\text{work/female})$
- Are having an injury at work and being a female independent events? Why?
- Is the event that an injured person is male independent of the event that an injured person was hurt at home?

Class Notes: Prof. G. Battaly, Westchester Community College, NY

 [Statistics Home Page](#)

©Gertrude Battaly, 2010

 [Class Notes](#)

4.6 Independence

p. 203 # 116

	Location of injury			Total
	Work	Home	Other	
Male	8	9.8	17.8	35.6
Female	1.3	11.6	12.9	25.8
Total	9.3	21.4	30.7	61.4

$$a) P(W) = \frac{9.3}{61.4} = 0.151$$

$$b) P(W/F) = \frac{1.3}{25.8} = 0.050$$

c) W, F independent?

$$P(W) = 0.151 \neq 0.050 = P(W/F)$$

DEPENDENT

Class Notes: Prof. G. Battaly, Westchester Community College, NY

[Statistics Home Page](#)

©Gertrude Battaly, 2010

[Class Notes](#)

4.6 Independence

p. 203 # 116

	Location of injury			Total
	Work	Home	Other	
Male	8	9.8	17.8	35.6
Female	1.3	11.6	12.9	25.8
Total	9.3	21.4	30.7	61.4

M, H dependent or independent?

$$P(H/M) \stackrel{?}{=} P(H) \quad \Bigg| \quad P(M/H) \stackrel{?}{=} P(M)$$

$$P(H) = \frac{21.4}{61.4} = 0.349$$

$$P(H) \neq P(H/M)$$

$$P(H/M) = \frac{9.8}{35.6} = 0.275 \therefore H \text{ and } M \text{ are}$$

$$P(H/M) = 0.275 \neq 0.349 = P(H) \text{ dependent}$$

not independent

Class Notes: Prof. G. Battaly, Westchester Community College, NY

4.6 Independence

Q. 204 #120

roll 2 dice



$6 \cdot 6 = 36$
equally likely.

A = red, even

B = black, odd.

Are A, B independent?

$P(A|B) = P(A)$ independent.

$$P(A) = \frac{3}{6} = \frac{1}{2}$$

$$P(A|B) = \frac{3}{6} = \frac{1}{2}$$

$$P(A|B) = P(A)$$

$\therefore A, B$ INDEPENDENT